

Theoretical Reevaluation of the π -Donating Effect of Electron-Withdrawing Substituents in the Conjugated Cationic Systems

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The π -donating effects of acceptor substituents are investigated theoretically using the high-level ab initio calculations for the isodesmic reactions, $X-(CH=CH)_n-CH_3 + (CH_2=CH)_n-CH_2^+ \rightarrow X-(CH=CH)_n-CH_2^+ + (CH_2=CH)_n-CH_3$ where $n = 1$ and 2 and $X = NH_2, OCH_3, F, H, Cl, CHO, CF_3, CN,$ and NO_2 . Electron delocalization is enhanced in the cationic systems and also by accounting for electron-correlation effect. The reaction energies (ΔH°), bond-length changes (Δd), and electronic charge shifts (Δq_π) do not provide a reliable measure of the π -donating ability of the acceptor substituents. In contrast, the percentage contribution of resonance structures (wt %) by the natural resonance theory (NRT) analysis and the energy changes due to deletion of the relevant π orbitals (ΔE_D) are the better methods of evaluating the π -donating behaviors. Proper accounting of the stabilization energies due to π -donation by the electron acceptors in the conjugated cationic species is only possible with the high-level correlated methods. In contrast to the earlier reports that the two strong acceptors, $X = CF_3$ and NO_2 , have some π -donating ability under strong π -electron demand conditions, the NRT and ΔE_D analyses do not support such an effect. We conclude that the π -donating effect of π -acceptors increases in the order $X = CHO < CN < Cl$. Stabilization of the correlated energies with $X = CF_3$ and NO_2 is almost entirely due to $n-\sigma^*$ -type charge-transfer delocalization.

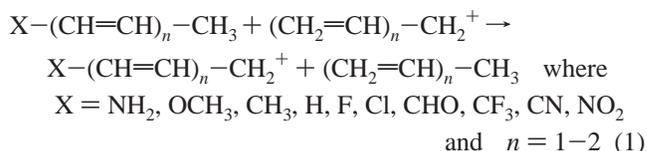
Introduction

The substituent effects on the reaction mechanisms and reactivities have been extensively studied, and general characteristics of the substituent effects have been well-established long ago. However, the fact that substituents known as typical π -acceptors such as CN and CHO can act as π -donors in cationic species has been reported theoretically¹ as well as experimentally.² For example, Paddon-Row et al.^{1a} have shown that formyl and cyano substituents operate as π -donors in unconjugated cationic species, $R^1(R^2)C^+-X$ (R^1 and $R^2 = H$ or alkyl and $X = CN, CHO,$ or CF_3) through ab initio calculations with the STO-3G and 4-31G basis sets. Similar results have also been reported by Reynolds et al.^{1b} for conjugated and aromatic cationic species, $XCH=CHCH_2^+$ and $XC_6H_4CH_2^+$. These theoretical works on the π -donating behaviors of the acceptors in the cationic species have been experimentally supported by the ¹³C NMR studies of the diaryl α -carbonyl cations, $(Ph)_2C^+-COR$.^{2a}

Notwithstanding, one fundamental problem as to the precise nature of the π -donating behavior of acceptors still remains because most of the earlier theoretical works have been carried out at uncorrelated Hartree–Fock levels with relatively small basis sets. Thus, the results of the earlier theoretical works may be inaccurate qualitatively as well as quantitatively, for example, CHO- and CF_3 -substituted methyl cations are not stable stationary species at the MP2 level,³ although Paddon-Row et al. in their work have concluded that the two substituents have π -donating characters.^{1a}

In this work, we have carried out high-level ab initio calculations using the complete basis set (CBS)⁴ and Gaussian-3

(G3)⁵ methods for the two hypothetical isodesmic hydride transfer reactions of conjugated cationic systems, eq 1, to



elucidate the π -donating effects of acceptors more precisely. However, the analyses of the pure π -donating behaviors of acceptors using the reaction energies only are probably not valid because the mutually compensating effects, that is, the favorable electron-donating and unfavorable accepting effects by the X-substituent, will be reflected in the reaction energies of eq 1. In other words, if the degree of π -accepting ability of the X-substituent is relatively larger than that of π -donating ability, the reaction energy will be highly unfavorable even though the absolute magnitude of the π -donating effect is substantial. The analyses using the π -charge densities can be also ambiguous because the calculated charge densities are largely dependent on the calculation methods as is well-known.⁶ In this work, we have analyzed further the π -donating behaviors of π -acceptors using the natural resonance theory (NRT)⁷ developed by Weinhold and co-workers together with the analyses using the energetics, charge densities, geometries, etc. The NRT method, which provides the relative weights of resonance structures, gives a reasonably quantitative description of the subtleties of electronic delocalization in a compact, chemically intuitive language.

Calculations

The Gaussian 98 program package⁸ with standard Pople-type basis sets was used throughout. All stationary point species in

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TABLE 1: The Calculated Reaction Enthalpies (ΔH° in kcal mol⁻¹) at 298 K for the Isodesmic Reactions with $n = 1$ in Eq 1

| X | RHF ^a | MP2 ^a | B3LYP ^a | CBS-Q | G3 | $\delta\Delta H^\circ$ ^b |
|------------------|------------------|------------------|--------------------|--------|--------|-------------------------------------|
| NH ₂ | -46.74 | -52.36 | -50.09 | -51.36 | -51.14 | -4.40 |
| OCH ₃ | -30.77 | -34.59 | -33.91 | -34.76 | -34.69 | -3.92 |
| CH ₃ | -13.35 | -14.43 | -16.37 | -15.25 | -15.27 | -1.92 |
| F | -2.71 | -5.62 | -6.56 | -5.85 | -5.18 | -2.47 |
| H | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| Cl | 0.67 | -5.70 | -6.21 | -7.93 | -8.17 | -8.84 |
| CHO | 13.41 | 9.38 | 9.90 | 10.44 | 10.43 | -3.26 |
| CF ₃ | 16.57 | 14.81 | 11.96 | 15.80 | 14.94 | -1.63 |
| CN | 19.74 | 14.77 | 12.28 | 12.17 | 14.21 | -5.53 |
| NO ₂ | 31.74 | 20.72 | 19.34 | 19.45 | 19.86 | -11.88 |

^a 6-31G* basis set was used. ^b $\delta\Delta H^\circ = \Delta H^\circ_{G3} - \Delta H^\circ_{RHF}$.

the hypothetical isodesmic hydride transfer reactions, eq 1, were fully optimized and were verified by the vibrational frequency calculations⁹ at the RHF, B3LYP,¹⁰ and MP2¹¹ levels with the 6-31G* basis set.¹² The calculated energies were further refined by the modified CBS-Q⁴ and Gaussian-3 (G3)⁵ methods for the reactions with $n = 1$ in eq 1 using the optimized geometries and thermochemical properties obtained at the MP2 level. For the reactions with $n = 2$ in eq 1, the calculations were limited up to the modified CBS-4 level⁴ because CBS-Q and G3 calculations require enormous computational time and cost for the large reaction systems with more than five non-hydrogen atoms. The natural bond orbital (NBO)¹³ and natural resonance theory (NRT)⁷ analyses were also carried out using the NBO-4M program¹⁴ interfaced to the Gaussian 98 program.

Results and Discussion

(A) Energetics. The reaction enthalpies, ΔH° , for the hypothetical isodesmic reactions with $n = 1$ in eq 1 calculated at various theoretical levels are summarized in Table 1. The zero-point-corrected electronic energies (E_{ZPE})¹⁵ of the neutral and cationic species are collected in Supporting Information (S1). It is generally known that the reaction energies of isodesmic reactions such as eq 1 are reproduced well even by simple computational methods¹⁶ because the changes in the electron correlation energies are usually small because of the conservation of the number of bonds of equal types in reactants and products. However, examination of Table 1 shows that the ΔH° values obtained at the uncorrelated restricted Hartree-Fock (RHF) level are generally less exothermic or more endothermic than those at the correlated levels, that is, inclusion of electron correlation energies generally lowers the reaction enthalpies ($\delta\Delta H^\circ = \Delta H^\circ_{\text{corr}} - \Delta H^\circ_{\text{RHF}} < 0$) as shown for $\delta\Delta H^\circ = \Delta H^\circ_{G3} - \Delta H^\circ_{\text{RHF}}$ in Table 1.

Nevertheless, it is not certain whether the results of $\delta\Delta H^\circ < 0$ were solely caused by the electron correlation effects, because, as is well-known, the results obtained by the CBS and G3 calculations include the mixed basis set effects. So, we have examined the basis set effects on the reaction energies (ΔE), and the results are collected in Table 2. However, as can be seen in Table 2, the variations of ΔE by basis set changes are, in general, small within 1.2 kcal mol⁻¹ excepting for X = Cl, CHO, and NO₂ indicating that the basis set effects are relatively smaller than the electron correlation effects. For example, in the case of X = CN, $\delta\Delta E$ ($= \Delta E(\text{RHF}/6-311+\text{G}(3\text{d}2\text{f},2\text{d}\text{f},2\text{p}) - \Delta E(\text{RHF}/6-31\text{G}^*))$), which reflects the effect of the larger basis set, is only 0.54 kcal mol⁻¹ (Table 2). Whereas $\delta\Delta H^\circ$ ($= \Delta H^\circ_{G3} - \Delta H^\circ_{\text{RHF}}$), which includes both of the basis set and electron correlation effects, is -5.53 kcal mol⁻¹ (Table 1). Even in the case X = Cl, $\delta\Delta H^\circ$ is -8.84 kcal mol⁻¹ but $\delta\Delta E$ is only

TABLE 2: The Electronic Energy Changes (ΔE in kcal mol⁻¹) for the Isodesmic reactions with $n = 1$ in Eq 1 Obtained at the RHF Level^a

| X | 6-311+ | | | | |
|------------------|--------|---------|--------------|----------------|-------------------------------|
| | 6-31G* | 6-31+G* | 6-31G(2df,p) | G(3d2f,2df,2p) | $\delta\Delta E$ ^b |
| NH ₂ | -47.65 | -47.03 | -47.68 | -47.17 | 0.66 |
| OCH ₃ | -31.19 | -31.02 | -32.02 | -31.73 | -0.51 |
| CH ₃ | -13.08 | -13.53 | -13.59 | -14.21 | -1.05 |
| F | -2.95 | -1.65 | -4.51 | -3.10 | -0.14 |
| H | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| Cl | 0.54 | -0.31 | -0.95 | -2.35 | -2.99 |
| CHO | 13.89 | 14.95 | 13.58 | 15.04 | 2.03 |
| CF ₃ | 16.87 | 18.22 | 15.38 | 17.80 | 1.13 |
| CN | 20.39 | 20.50 | 20.26 | 20.59 | 0.54 |
| NO ₂ | 42.77 | 43.18 | 39.77 | 40.84 | -1.93 |

^a Single point calculations using MP2/6-31G* geometry. ^b $\delta\Delta E = \Delta E_{\text{RHF}/6-311+\text{G}(3\text{d}2\text{f},2\text{d}\text{f},2\text{p})} - \Delta E_{\text{RHF}/6-31\text{G}^*}$.

-2.99 kcal mol⁻¹, albeit the $\delta\Delta E$ of X = Cl is the largest among those studied in this work. It appears, therefore, that the electron correlation effects are much more important than the basis set effects in the reactions of eq 1.

On the other hand, we note that all substituents irrespective of whether they are electron donors ($\delta\sigma < 0$) or acceptors ($\delta\sigma > 0$) stabilize ($\delta\Delta H^\circ < 0$) the cationic form more than the neutral-substituted conjugated system, eq 1, when calculated at the correlated levels. The greater stabilization due to inclusion of electron correlation is seen to result not only from a stronger donor (X = NH₂, $\delta\Delta H^\circ = -4.62$ kcal mol⁻¹) but also from a stronger acceptor (X = NO₂, $\delta\Delta H^\circ = -12.29$ kcal mol⁻¹). We emphasize that electron correlation enhances all types of resonance delocalization, not only the π -type but also the σ -type, leading to energy stabilization. Conspicuous, unexpectedly large stabilizations are those for X = Cl ($\delta\Delta H^\circ = -8.84$ kcal mol⁻¹) and X = CN ($\delta\Delta H^\circ = -5.53$ kcal mol⁻¹). The smallest stabilization is found for X = CF₃ ($\delta\Delta H^\circ = -1.63$ kcal mol⁻¹). These stabilizations ($\delta\Delta H^\circ < 0$) upon hydride transfer forming the cationic conjugated system should include contributions such as (i) enhanced π -delocalization (structures **1b** and **1c**, Scheme 1) for π -donors and (ii) enhanced delocalization due to all other types of (e.g., proximate σ - σ^* including n - σ^* , π - σ^* , σ - π^* , etc.)¹⁷ orbital interactions (included in structure **1a**, Scheme 1) for π -acceptors. Therefore, the $\delta\Delta H^\circ$ values do not represent the π -donating effect (structure **1c**) alone (but also include the σ delocalization effect) so that they are not a reliable measure for assessing the π -donating ability of the π -acceptors. Also, the relative orders of ΔH° by the RHF method are different from those of the correlated levels, for example, the ΔH° value for X = CF₃ is less endothermic by 3.17 kcal mol⁻¹ at the RHF level but is more endothermic by 0.73 kcal mol⁻¹ at the G3 level than that for R = CN. This indicates that the electron correlation effects are very important even for the typical isodesmic reactions, eq 1. Nevertheless, general trends of reaction enthalpies obtained at the RHF/6-31G* level are similar to those obtained at the correlated levels excepting a few cases as mentioned above. Therefore, unless higher accuracy is required, the results obtained at the RHF/6-31G* level will be sufficient.

On the other hand, the absolute ΔH° values obtained at the correlated levels, MP2, B3LYP, CBS-Q, and G3 levels, are very similar within about ± 2.6 kcal mol⁻¹. Especially, the ΔH° values at the MP2 and G3 levels are very similar excepting only X = Cl. The relatively large difference in the X = Cl is mainly caused by the difference of basis sets between the MP2/6-31G* and G3 levels rather than the correlation effects. The

TABLE 4: Percentage Weights (wt %) of the Resonance Structures in the Cationic Species with $n = 1$ Obtained by the NRT Analyses

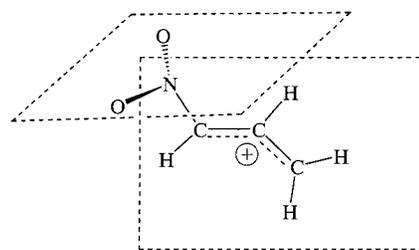
| X | RHF | | | MP2 | | |
|------------------|------|------|------|------|------|------|
| | Ia | Ib | Ic | Ia | Ib | Ic |
| NH ₂ | 16.7 | 54.9 | 16.9 | 15.7 | 41.6 | 17.8 |
| OCH ₃ | 20.7 | 56.2 | 11.7 | 18.2 | 40.6 | 12.5 |
| CH ₃ | 38.3 | 54.0 | 2.4 | 33.1 | 44.2 | 3.7 |
| F | 36.1 | 52.2 | 4.6 | 31.8 | 44.2 | 5.6 |
| H | 48.5 | 48.5 | 0.0 | 45.2 | 45.2 | 0.0 |
| Cl | 37.0 | 46.3 | 6.5 | 29.9 | 38.3 | 8.7 |
| CHO | 45.5 | 43.6 | 1.2 | 35.6 | 33.9 | 2.8 |
| CF ₃ | 44.2 | 37.2 | 0.0 | 32.5 | 29.9 | 0.0 |
| CN | 46.3 | 43.0 | 2.6 | 34.4 | 32.9 | 4.7 |

the π -donating effect in the neutral molecule is actually much smaller compared to that of the π -accepting effect. On the other hand, the magnitude of ΔE_D increases in the order X = CHO < X = CN < X = Cl for both the cationic and neutral species. This means that the π -donating effect of X = Cl is the largest among the π -acceptors studied in this work. The largest π -donating effect of X = Cl can be rationalized by the fact that the π -electrons involved in X = Cl are 3p lone-pair electrons, whereas those in X = CHO and CN are the 2p π -bonding orbital electrons. Therefore, the flow of electron densities from X to the π^* -orbital of the substrate will be much larger for X = Cl than for X = CHO or CN because (i) lone-pair electrons are, in general, loosely bound compared to bonding electrons and (ii) the energy level of the 3p lone-pair orbital on X = Cl is higher compared to that of the 2p bonding π -orbitals in X = CHO or CN so that the charge-transfer stabilization energies, $\Delta E_{ct} \approx -F_{\pi\pi^*}^2/\Delta\epsilon$ where $\Delta\epsilon = \epsilon_{\pi^*} - \epsilon_{\pi}$ and $F_{\pi\pi^*}$ is the Fock matrix element, are larger. This is confirmed by $\Delta\epsilon$ and $F_{\pi\pi^*}$ values collected in Table 4; the energy level gaps, $\Delta\epsilon$, between two interacting orbitals in the cationic species increase in the order X = Cl < X = CN < X = CHO, but $F_{\pi\pi^*}$ increases in the reverse order at the NBO-RHF/6-31G*/MP2/6-31G* level.

The order of the π -donating effects by electron-withdrawing substituents estimated from the ΔE_D is consistent with the results of the NRT analyses. The percentage weights (wt %) of three important resonance structures representing the delocalization of cationic charge densities in the cationic species as shown in Scheme 1 are calculated by the NRT analysis⁷ at RHF and MP2 levels as summarized in Table 4. The resonance structure of **Ic** reflects the π -donating effect of the X-substituent, and hence, the weight percent of the structure **Ic** is a measure of the π -donating effect. Therefore, in these NRT analyses, the resonance structures of **Ia** and **Ib**, which correspond to the sigma-inductive resonance structures, were chosen as the reference structures to compare with the weight percent of the resonance structure **Ic** and show the π -donating effects by X-substituents.

Reference to this table reveals that weight percents of the relatively short-range delocalized forms, **Ia** and **Ib**, are higher in the RHF than in the MP2 level results while that of the longer chain form (**Ib**) with a greater delocalized structure is higher in the MP2 than in the RHF results. This is again in keeping with the general trends of enhanced delocalized structures due to inclusion of electron correlation effect. In the NRT analyses, both the absolute magnitude of wt % (**Ic**) and relative ratios, wt % (**Ic**)/wt % (**Ia**) and wt % (**Ib**)/wt % (**Ia**), increase in the order CHO < CN < Cl.

However, in the calculations of the ΔE_D , we have excluded the species with X = NO₂ because the X = NO₂ and the substrate fragment in the cationic species are nearly perpen-

SCHEME 3**TABLE 5: The Calculated Reaction Enthalpies (ΔH° in kcal mol⁻¹) at 298 K for the Isodesmic Reactions with $n = 2$ in Eq 1**

| X | RHF ^a | MP2 ^a | B3LYP ^a | CBS-4 | $\delta\Delta H^\circ$ ^b |
|------------------|------------------|------------------|--------------------|--------|-------------------------------------|
| NH ₂ | -33.20 | -36.65 | -34.72 | -36.22 | -3.02 |
| OCH ₃ | -20.33 | -22.32 | -22.08 | -21.84 | -1.51 |
| CH ₃ | -8.57 | -8.94 | -10.18 | -9.60 | -1.03 |
| F | -0.54 | -2.22 | -3.20 | -3.37 | -2.83 |
| H | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| Cl | 3.02 | -1.16 | -1.65 | -3.87 | -6.89 |
| CHO | 12.11 | 8.98 | 10.32 | 8.97 | -3.14 |
| CF ₃ | 13.29 | 11.84 | 10.44 | 11.85 | -1.44 |
| CN | 17.35 | 13.13 | 12.76 | 10.80 | -6.55 |
| NO ₂ | 25.07 | 17.59 | 20.03 | 19.88 | -5.19 |

^a 6-31G* basis set was used. ^b $\delta\Delta H^\circ = \Delta H^\circ_{\text{CBS4}} - \Delta H^\circ_{\text{RHF}}$.

dicular each other as represented in Scheme 3. Indeed, the planar structure is not a stable stationary species with one imaginary frequency at the uncorrelated RHF/6-31G* as well as the correlated MP2/6-31G* and B3LYP/6-31G* levels. According to the normal-mode analysis, the one imaginary frequency of the planar structure corresponds to a rotational mode leading to the perpendicular structure. Therefore, the X = NO₂ in the reaction systems with $n = 1$ cannot act structurally as a π -donor, although Reynolds et al.^{1b} in their work have classified X = NO₂ as a π -donor comparable to X = CH₃. The perpendicular structure in the cationic species with X = NO₂ is formed for the sake of minimizing the unfavorable electron-accepting effect by stronger π -acceptor, X = NO₂, from the electron-deficient cationic center. This shows that the π -donating effect of X = NO₂ is actually a minor effect (or nonexistent), which is overwhelmed by a strong electron-withdrawing power, because if the π -donating effect of X = NO₂ is larger than the accepting effect, the structure of the cationic species with X = NO₂ will be planar so as to acquire the maximum stabilization energies by the π -donating effects.

To compare the strength of π -donating effect by π -acceptors in the reactions with varying π -electron chain length, the hypothetical isodesmic reactions with $n = 2$ in eq 1 are also investigated and the reaction enthalpies, ΔH° , are summarized in Table 4. Although the levels of calculation for the reaction systems with $n = 2$ are limited up to the CBS-4 level because of the size of the reaction systems, energetics at the CBS-4 level should provide more accurate and more reliable results than those obtained at the MP2 and B3LYP levels as discussed above. The relative orders of ΔH° predicted at the CBS-4 level for X = CF₃ and CN and for X = F and Cl are consistent with those at the CBS-Q and G-3 levels for $n = 1$ (Table 1). However, for those at the lower levels, RHF, MP2, and B3LYP, the relative orders are reversed so that the predictions at the lower-level correlated methods are unreliable.

Examination of Table 5 shows that the trends of the reaction enthalpies obtained at the CBS-4 level for the reactions with $n = 2$ are very similar to those for the reactions with $n = 1$. However, the absolute magnitudes of the reaction enthalpies,

TABLE 6: Calculated Bond Lengths (d in Å) of the Reactions with $n = 1$ at the MP2/6-31G* Level
$$\text{X}^{\text{d}_3}\text{-CH}^{\text{d}_2}\text{=CH}^{\text{d}_1}\text{-CH}_3$$

| X | neutral | | | cation | | | Δd^a | | |
|------------------|---------|--------|--------|--------|--------|--------|--------------|--------------|--------------|
| | d_1 | d_2 | d_3 | d_1 | d_2 | d_3 | Δd_1 | Δd_2 | Δd_3 |
| NH ₂ | 1.4991 | 1.3426 | 1.3512 | 1.4302 | 1.3006 | 1.4062 | -0.1479 | +0.0876 | -0.1056 |
| OCH ₃ | 1.5005 | 1.3425 | 1.3563 | 1.4239 | 1.2274 | 1.3662 | -0.1442 | +0.0814 | -0.1388 |
| CH ₃ | 1.4997 | 1.3396 | 1.3731 | 1.3982 | 1.4598 | 1.4998 | -0.1266 | +0.0586 | -0.0400 |
| F | 1.4982 | 1.3308 | 1.3682 | 1.3944 | 1.2820 | 1.3581 | -0.1300 | +0.0636 | -0.0761 |
| H | 1.4996 | 1.3378 | 1.3836 | 1.3836 | 1.0876 | 1.0851 | -0.1160 | +0.0458 | +0.0025 |
| Cl | 1.4985 | 1.3353 | 1.3691 | 1.4023 | 1.6398 | 1.7344 | -0.1294 | +0.0670 | -0.0946 |
| CHO | 1.4945 | 1.3448 | 1.3838 | 1.3872 | 1.5060 | 1.4684 | -0.1107 | +0.0425 | +0.0376 |
| CF ₃ | 1.4958 | 1.3372 | 1.3857 | 1.3814 | 1.5172 | 1.4866 | -0.1101 | +0.0442 | +0.0031 |
| CN | 1.4945 | 1.3448 | 1.3832 | 1.3929 | 1.4130 | 1.4319 | -0.1113 | +0.0481 | -0.0189 |
| NO ₂ | 1.4938 | 1.3337 | 1.3626 | 1.4079 | 1.4234 | 1.4571 | -0.1312 | +0.0742 | -0.0337 |

^a $\Delta d = d(\text{cation}) - d(\text{neutral})$.

TABLE 7: Calculated Bond Lengths (d in Å) of the Reactions with $n = 2$ at the MP2/6-31G* Level
$$\text{X}^{\text{d}_5}\text{-CH}^{\text{d}_4}\text{=CH}^{\text{d}_3}\text{-CH}^{\text{d}_2}\text{=CH}^{\text{d}_1}\text{-CH}_3$$

| X | neutral | | | | | cation | | | | |
|------------------|---------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| | d_1 | d_2 | d_3 | d_4 | d_5 | d_1 | d_2 | d_3 | d_4 | d_5 |
| NH ₂ | 1.4978 | 1.3476 | 1.4501 | 1.3506 | 1.3974 | 1.3525 | 1.4337 | 1.3694 | 1.4112 | 1.3103 |
| OCH ₃ | 1.4978 | 1.3469 | 1.4530 | 1.3498 | 1.3609 | 1.3557 | 1.4276 | 1.3777 | 1.4019 | 1.2882 |
| CH ₃ | 1.4972 | 1.3467 | 1.4544 | 1.3467 | 1.4972 | 1.3623 | 1.4159 | 1.3982 | 1.3773 | 1.4743 |
| F | 1.4970 | 1.3460 | 1.4535 | 1.3377 | 1.3552 | 1.3629 | 1.4154 | 1.3941 | 1.3729 | 1.3005 |
| H | 1.4971 | 1.3462 | 1.4559 | 1.3445 | 1.0847 | 1.3662 | 1.4098 | 1.4098 | 1.3662 | 1.0861 |
| Cl | 1.4964 | 1.3469 | 1.4527 | 1.3426 | 1.7299 | 1.3631 | 1.4158 | 1.3949 | 1.3797 | 1.6641 |
| CHO | 1.4951 | 1.3485 | 1.4481 | 1.3525 | 1.4637 | 1.3683 | 1.4085 | 1.4100 | 1.3709 | 1.4882 |
| CF ₃ | 1.4956 | 1.3469 | 1.4521 | 1.3440 | 1.4849 | 1.3691 | 1.4069 | 1.4133 | 1.3634 | 1.5088 |
| CN | 1.4951 | 1.3481 | 1.4485 | 1.3526 | 1.4280 | 1.3691 | 1.4082 | 1.4089 | 1.3758 | 1.4179 |
| NO ₂ | 1.4945 | 1.3480 | 1.4480 | 1.3413 | 1.4509 | 1.3697 | 1.4072 | 1.4116 | 1.3625 | 1.4583 |

$|\Delta H^\circ|$, are smaller for the reactions with $n = 2$ than those with $n = 1$ (Tables 1 and 5), indicating that the effects of X-substituents are relatively weaker for the reactions with $n = 2$. These results reflect that the π -electron demand is weaker because the π -electron densities of the species with $n = 2$ are more abundant relative to the cationic species with $n = 1$. This is confirmed by the magnitude of ΔE_D collected in Table 3. As can be seen in Table 3, the magnitudes of ΔE_D in the two neutral species with $n = 1$ and 2 are nearly same indicating that the π -effect is independent of the chain length of the π -system. However, the magnitudes of ΔE_D are much larger in cationic species with $n = 1$ than $n = 2$. This is caused by weaker π -electron demand in cationic species with $n = 2$ than in those with $n = 1$. Consequently, the magnitude of $\delta\Delta E_D$ for the reactions with $n = 2$ is about half of those with $n = 1$, that is, the π -donating effect of π -acceptors has diminished in the reaction systems with $n = 2$, as expected. Nevertheless, the relative order of magnitude for the $\delta\Delta E_D$ is the same for both systems with $n = 1$ and 2. Thus, it can be concluded that the π -donating effect of π -acceptors increases in the order CHO < CN < Cl.

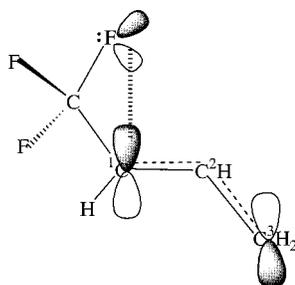
(B) Structures. The bond lengths (d) optimized at the MP2/6-31G* level are summarized in Tables 6 and 7. For the reactions with $n = 1$, the variations of bond lengths of d_2 with X-substituents in neutral species are much smaller than those in the cationic species. This indicates that the effects of X-substituents on the bond lengths are larger in cationic species. However, any simple relationships between the bond length, d_2 , and a physical property of the X-substituent could not be found in both neutral and cationic species. Close examination of Table 6 reveals that for all substituents (X) the bond length of d_1 contracts, while that of d_2 stretches in the cationic species as expected from the resonance structure **Ib**. The contraction

of d_1 is, however, greater than the stretching of d_2 , reflecting the greater contribution of **Ib** than **Ia**. The NRT analysis in Table 4 confirms the greater contribution of **Ib** than **Ia** only for π -donors, X = NH₂, OCH₃, CH₃, F, and Cl, but not for π -acceptors, X = CHO, CF₃, and CN. Thus, the geometrical changes upon hydride transfer are not simply related to the π -donating ability alone. This is true with the bond length changes of d_3 , which should reflect the contribution of structure **Ic**. If the structure **Ic** contributes substantially, d_3 should contract. This is evident with all of the normal π -donors, but there are anomalies with π -acceptors: for X = CHO and CF₃, d_3 stretches, while for X = Cl, CN, and NO₂, it contracts. The NRT (Table 4), as well as ΔE_D (Table 3), analysis shows that for electron-withdrawing substituents structure **Ic** contributes in the cationic species with X = Cl, CHO, and CN but not in those with X = CF₃ and NO₂. This again demonstrates the unreliability of the geometrical changes as a measure of the pure π -electronic effects. The bond-length changes in the $n = 2$ systems (Table 7) also show similar behavior to that exhibited in the $n = 1$ systems. These results are somewhat different from those reported by Reynolds et al.,^{1b} in which X = CF₃ was shown to have some π -donating ability. Therefore, we have further analyzed the π -electron densities for X-substituents and substrate fragments, $q_\pi(\text{X})$ and $q_\pi(\text{sub})$, in the neutral and cationic forms with $n = 1$, and the results are summarized in Table 8. The $q_\pi(\text{X})$ value decreases ($\Delta q_\pi(\text{X}) < 0$) gradually, while the $q_\pi(\text{sub})$ value increases ($\Delta q_\pi(\text{sub}) > 0$) as the π -electron-donating power of the X-substituent becomes larger. Especially, for X = Cl, CN, and CHO moieties, the $q_\pi(\text{X})$ values in the neutral species are larger indicating the π -electron accepting effects of the substituents, X. However, the $q_\pi(\text{X})$ values for X = Cl, CHO, and CN in the cationic forms decrease reflecting that the π -electron densities flow out from the

TABLE 8: Calculated π -Electron Densities (q_π in Electron Unit)^a Obtained by the Natural Population Analysis (NPA) at the MP2 Level

| X | neutral | | cation | | $\Delta q_\pi(X)$ | $\Delta q_\pi(\text{sub})$ |
|------------------|------------|-----------------------|------------|-----------------------|-------------------|----------------------------|
| | $q_\pi(X)$ | $Q_\pi(\text{sub})^b$ | $q_\pi(X)$ | $Q_\pi(\text{sub})^b$ | | |
| NH ₂ | 1.719 | 2.090 | 1.458 | 2.503 | -0.261 | 0.413 |
| OCH ₃ | 1.821 | 2.098 | 1.561 | 2.400 | -0.260 | 0.302 |
| CH ₃ | | 1.999 | | 2.099 | | 0.100 |
| F | 1.908 | 2.052 | 1.772 | 2.192 | -0.136 | 0.140 |
| H | | 1.993 | | 1.992 | | -0.001 |
| Cl | 1.909 | 2.050 | 1.650 | 2.308 | -0.261 | 0.258 |
| CHO | 2.059 | 1.926 | 1.938 | 2.039 | -0.121 | 0.113 |
| CF ₃ | | 1.972 | | 2.019 | | 0.047 |
| CN | 2.018 | 1.968 | 1.857 | 2.121 | -0.161 | 0.153 |

^a The π -electron densities are obtained by the electron densities of $2p_z$ and $3p_z$ orbitals for 1st and 2nd row elements, respectively, in the NPA analysis. ^b Sum of the π -electron densities in the substrate fragment.

SCHEME 4

X-substituent to the substrate moiety. The magnitudes of $\Delta q_\pi(X)$ and $\Delta q_\pi(\text{sub})$ increase in the order $X = \text{CHO} < X = \text{CN} < X = \text{Cl}$. This is in line with the orders of π -donating ability predicted by the NRT and ΔE_D analyses. However, interestingly, the $\Delta q_\pi(\text{sub})$ for $X = \text{CF}_3$ is $+0.047e$. This suggests that the π -electron density in the substrate fragment increases by the π -electron donating effect of $X = \text{CF}_3$. The putative π -electron donating effect of $X = \text{CF}_3$ seems, however, somewhat strange because there are no π lone-pair electrons or other π -orbitals that can directly conjugate with the π^* -orbital of the substrate fragment existing in the C-atom of $X = \text{CF}_3$. Although $X = \text{CF}_3$ could act as a hyperconjugative π -electron donor as evidenced with $X = \text{CH}_3$, the other possible way would be through-space interaction between lone-pairs of the F-atom and the π^* -orbital of the substrate fragment as shown in Scheme 4. Nevertheless, such π -donating behavior is inconsistent with our NRT and ΔE_D analyses. The through-space interaction as shown in Scheme 4 should be very weak because the distance between the C¹-atom and the F-atom is relatively far (2.36 Å). The increase in the substrate π -electron density for $X = \text{CF}_3$ ($\Delta q_\pi(\text{sub}) > 0$) in the cationic form, therefore, comes most likely from other proximate $\sigma-\pi^*$ -type charge-transfer delocalizations. Therefore, it is expected that the π -electron-donating effect of $X = \text{CF}_3$ is not important, and the trend shown by the electron transfer, Δq_π , involved in the cationic species is also not a good measure of the π -donating ability.

This expectation is confirmed by the proximate bond-antibond (including all types of $n-\pi^*$, $n-\sigma^*$, $\sigma-\sigma^*$, etc.) delocalization energies (ΔE_{del}) between X and the substrate fragments. The delocalization energies are obtained by zeroing all of the off-diagonal elements of the common block between X and the substrate in the Fock matrix using the NBO method,¹³ and the results are summarized in Table 9. As can be seen in Table 9, total delocalization energies ($\Delta E_{\text{del}}(\text{T})$), as well as partial delocalization energies ($\Delta E_{\text{del}}(\text{X})$), which are caused by

TABLE 9: Delocalization Energies (ΔE_{del} in kcal mol⁻¹) between the X-Substituent and the Substrate Fragment Calculated at the RHF/6-31G*/MP2/6-31G* Level

| X | $\Delta E_{\text{del}}(\text{T})^a$ | $\Delta E_{\text{del}}(\text{X})^b$ | $\delta \Delta E_{\text{del}}(\text{X})^c$ |
|-----------------|-------------------------------------|-------------------------------------|--|
| Cl | 81.1 | 77.5 | 77.5 |
| CHO | 38.0 | 22.3 | 13.8 |
| CF ₃ | 35.7 | 18.1 | -2.9 |
| CN | 68.4 | 37.5 | 29.9 |

^a Total delocalization energies between the X-substituent and the substrate fragment. ^b Partial delocalization energies due to charge transfer from the X-substituent to the substrate. ^c Delocalization energies excluding contributions of the $n-\sigma^*$ interactions between $n(\text{X})$ and $\sigma^*(\text{C}-\text{X})$ orbitals.

the delocalization of one direction from X to the substrate fragment, increase in the order $X = \text{CF}_3 < X = \text{CHO} < X = \text{CN} < X = \text{Cl}$. This order is consistent with the predicted π -donating abilities of X-substituents discussed above. Nevertheless, the relative magnitudes of the delocalization energies, $\Delta E_{\text{del}}(\text{T})$ and $\Delta E_{\text{del}}(\text{X})$, for $X = \text{CF}_3$ are very similar to those for $X = \text{CHO}$. Examination of Table 8 reveals that the charge transfer occurs almost entirely from the $n_{\text{F}}-\sigma^*_{\text{C}-\text{C}}$ -type interaction^{7,13,21b} for $X = \text{CF}_3$ whereas it comes from other types of proximate charge delocalizations, for example, $\pi-\pi^*$, $n-\pi^*$, $\sigma-\sigma^*$, etc., rather than $n_{\text{X}}-\sigma^*_{\text{C}-\text{C}}$ for $X = \text{Cl}$, CHO , and CN .^{7,13,21b} Thus, if the contributions of the $n-\sigma^*$ interactions are deleted, the net delocalization ($\delta \Delta E_{\text{del}}(\text{X})$) from X to the substrate fragment, and hence the net stabilization by the substituent $X = \text{CF}_3$, will be nearly zero. Once again, this result indicates that the π -donating ability of $X = \text{CF}_3$ is not real. A similar interpretation of the net energy stabilization by $X = \text{NO}_2$ ($\delta \Delta H^\circ = -12.29$ kcal mol⁻¹ in Table 1) can be offered, that is, other (than $\pi-\pi^*$) types of proximate charge-transfer interactions (generally expressed as $\sigma-\sigma^*$ -type) stabilize the correlated energies of the cationic species.

Summary and Conclusion

The π -donating effect of π -acceptor substituents increases in the order $X = \text{CHO} < X = \text{CN} < X = \text{Cl}$ under a strong electron demand as in the conjugated correlated levels. Inclusion of electron correlation energies, in general, lowers the reaction enthalpies ($\delta \Delta H^\circ = H_{\text{corr}}^\circ - H_{\text{RHF}}^\circ < 0$) as shown for $\delta \Delta H^\circ = H_{\text{G}_3}^\circ - H_{\text{RHF}}^\circ$ in Table 1. All substituents, irrespective of whether they are electron donors ($\delta \sigma < 0$) or acceptors ($\delta \sigma > 0$), stabilize ($\delta \Delta H^\circ < 0$) the cationic form relative to the neutral-substituted conjugated system, eq 1, when calculated at the correlated levels. The greater stabilization due to inclusion of electron correlation is seen to result not only from a stronger donor ($X = \text{NH}_2$, $\delta \Delta H^\circ = -4.6$ kcal mol⁻¹) but from stabilization ($\delta \Delta H^\circ$) by the π -acceptors in the conjugated cationic systems. In contrast to the earlier reports that two strong acceptors, $X = \text{CF}_3$ and NO_2 , have some π -donating ability under strong π -electron demand, our NRT and ΔE_D analyses show no such π -donor effect by the two acceptor substituents; the stabilization of correlated energies with these two substituents is entirely caused by $n-\sigma^*$ -type charge-transfer interactions. In general, electron correlation enhances all types of delocalization (proximate $\sigma-\sigma^*$ charge-transfer interactions, which include $\pi-\pi^*$, $n-\pi^*$, $n-\sigma^*$, $\sigma-\sigma^*$, etc.) so that the studies involving electron delocalization are better suited to respectably high-level correlated rather than RHF level methods.

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Supporting Information Available: A table of electronic energies corrected for the zero-point vibrational energies. This material is available free of charge via the Internet at <http://pubs.acs.org>.

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